

# A framework for three-dimensional statistical shape modeling of the proximal femur in Legg-Calvé-Perthes disease

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## 24 1 Abstract

25 **Purpose:** The pathomorphology of Legg-Calvé-Perthes Disease (LCPD) is a key contributor to poor long-term  
 26 outcomes such as hip pain, femoroacetabular impingement, and early-onset osteoarthritis. Plain radiographs,  
 27 commonly used for research and in the clinic, cannot accurately represent the full extent of LCPD deformity. The  
 28 purpose of this study was to develop and evaluate a methodological framework for three-dimensional (3D) statistical  
 29 shape modeling (SSM) of the proximal femur in LCPD.

30 **Methods:** We developed a framework consisting of three core steps: segmentation, surface mesh preparation, and  
 31 particle-based correspondence. The framework aims to address challenges in modeling this rare condition,  
 32 characterized by highly heterogeneous deformities across a wide age range and small sample sizes. We evaluated  
 33 this framework by producing a SSM from clinical magnetic resonance images of 13 proximal femurs with LCPD  
 34 deformity from 11 patients between the ages of six and 12 years.

35 **Results:** After removing differences in scale and pose, the dominant shape modes described morphological features  
 36 characteristic of LCPD, including a broad and flat femoral head, high-riding greater trochanter, and reduced neck-  
 37 shaft angle. The first four shape modes were chosen for evaluation of the model’s performance, together describing  
 38 87.5% of the overall cohort variance. The SSM was generalizable to unfamiliar examples with an average point-to-  
 39 point reconstruction error below 1mm. We observed strong Spearman rank correlations (up to 0.79) between some  
 40 shape modes, 3D measurements of femoral head asphericity, and clinical radiographic metrics.

41 **Conclusion:** In this study we present a framework, based on SSM, for the objective description of LCPD deformity  
 42 in three dimensions. Our methods can accurately describe overall shape variation using a small number of  
 43 parameters, and are a step towards a widely accepted, objective 3D quantification of LCPD deformity.

44

45 Keywords: Legg-Calvé-Perthes Disease, hip joint, pediatrics, statistical shape modeling, morphology

## 46 2 Introduction

47 Legg-Calvé-Perthes Disease (LCPD) is a pediatric hip disorder characterized by avascular necrosis of the femoral  
 48 head (FH).[1] LCPD often results in a permanent residual deformity of the FH and secondary acetabular dysplasia,  
 49 which can manifest in features such as an enlarged, widened and sometimes flat FH, short femoral neck, a high-  
 50 riding greater trochanter, acetabular dysplasia, and hip joint incongruity. Patients with severe residual FH deformity  
 51 often present with hip pain, limited range of motion, and femoroacetabular impingement during adolescence.[2, 3]  
 52 Hip surgery is often indicated for these patients.[4, 5] An increased severity of residual FH deformity and acetabular  
 53 dysplasia at skeletal maturity (as described by the radiographic Stulberg classification[6]) is also associated with  
 54 greater risk of early-onset osteoarthritis (OA), with a reported rate of moderate-to-severe radiographic OA of more  
 55 than 40% in LCPD patients as young as 29 years at follow-up,[7] compared to only 2% in the 50-54 year old general  
 56 population.[8]

57 Quantifying the degree of LCPD deformity is an important part of patient assessment, treatment planning and  
 58 follow-up, but there are limitations to current approaches. Radiographic metrics do not accurately depict the full  
 59 extent of the pathomorphology of the deformity because they are based on planar projections of the three-  
 60 dimensional (3D) anatomy. These measurements are also sensitive to positioning errors between patients and  
 61 examinations, including difficulty in obtaining plain radiographs of true orthogonal views due to suboptimal leg  
 62 positioning that can be caused by decreased hip motion.[9, 10] Computed tomography provides 3D images of the  
 63 bones, but it requires considerable exposure to ionizing radiation and does not provide good visualization of soft  
 64 tissues, like articular cartilage overlying the bone. Magnetic resonance imaging (MRI) requires no ionizing radiation  
 65 and yields 3D images with good soft tissue visualization, making it suitable for ongoing follow-up imaging.  
 66 However, a major limitation of all 3D imaging is that there is currently no widely accepted, objective way by which  
 67 to quantify the 3D deformity in LCPD.

68 3D surface reconstructions from volumetric images have, however, been used to objectively describe anatomy and  
 69 anatomical variation through statistical shape modeling (SSM).[11–13] A key advantage of SSM is that it provides a  
 70 holistic representation of shape with independent continuous parameters (i.e., shape modes) without *a priori*  
 71 assumptions regarding measurements believed to be most clinically relevant. Previous applications of SSM in the  
 72 hip have included prediction of OA outcomes in older adults,[14, 15] identification of the most useful 2D clinical

73 measurements in cam-type femoroacetabular impingement syndrome,[16] and describing growth patterns in  
 74 pediatric hip disorders.[17, 18] It follows from these examples that SSM should provide the foundation for an open  
 75 and objective standard for describing 3D shape variation in LCPD. For such a foundation to be useful, it must  
 76 perform well when the available datasets are small and highly heterogeneous, which is typical for studies of LCPD  
 77 deformity.[19–21]

78 The accuracy and applicability of SSM relies fundamentally on the choice of landmark correspondences, particularly  
 79 in highly heterogeneous morphology such as LCPD deformity. Placing landmarks by hand is impractical for dense  
 80 point sets on 3D surfaces, and many automated methods rely on either brute force (e.g. matching closest nodes on  
 81 meshes) or geometric comparisons, both of which introduce suboptimal correspondences that can confound  
 82 statistical analysis.[22] Recently, entropy-particle-based methods for optimization of correspondence, as used in the  
 83 open-source SSM software *ShapeWorks*, have demonstrated excellent performance.[12, 23, 24] To facilitate  
 84 improved assessment of the long-term prognosis of this relatively rare condition, the present study extends entropy-  
 85 particle-based SSM methods to also include an incremental optimization routine.[25] This incremental approach was  
 86 designed to enable optimization of landmark correspondences when using a small, heterogeneous dataset.

87 The objectives of this study were to develop a framework for constructing expandable SSM of LCPD  
 88 pathomorphology, evaluate its accuracy and sensitivity to training population size, and illustrate its use to quantify  
 89 3D anatomical variation in a small cohort of LCPD patients.

### 90 3 Materials and Methods

91 The shape modeling framework presented herein consists of three key steps: segmentation, surface mesh  
 92 preparation, and particle-based correspondence. We present these steps below in the context of their application to  
 93 our evaluation cohort of 11 patients with LCPD, and the analyses used to evaluate the resulting SSM.

#### 94 3.1 Patients and Imaging

95 Eleven patients (eight male, three female) with LCPD were included in this Institutional Review Board approved  
 96 study (Table 1). Two patients had bilateral LCPD. Patient ages ranged from six to 12 years old (mean  $9 \pm 2$  years).  
 97 The modified Waldenstrom stages of LCPD progression[26] ranged from IIa (early fragmentation stage) to IV  
 98 (healed stage), and the modal stages were IIIa and IIIb (early and late reossification stages), containing four  
 99 proximal femurs each.

100

101 **Table 1: Patient demographics, natural history stage, and anatomical measurements.**

Subject	Gender	Age (yr.)	Side	Modified Elizabethtown stage	Asphericity (mm)	NSA (degrees)	ATD (mm)
1	Male	10	L	IV	2.3	126	16.8
2	Male	10	L	IIIb	2.9	134	31
3	Male	6	L	IIIb	3.6	130	19.2
			R	IIIa	3.5	131	17.3
4	Female	9	R	IIIb	4.8	132	9.9
5	Male	9	L	IIIa	4.0	141	32.3
6	Male	10	L	IIIb	5.1	140	19.1
			R	IIIa	5.4	135	12
7	Female	12	R	IIb	5.6	162	43.8
8	Male	12	R	IIIa	5.8	114	0
9	Male	11	L	IIa	2.7	132	14.8
10	Male	9	L	IIb	4.2	152	25.8
11	Female	8	R	IIa	2.7	131	15.4
<b>Total</b>						135.4	19.8
<b>[mean (SD)]:</b>		9 (2)			4.0 (1.2)	(11.8)	(11.2)

102

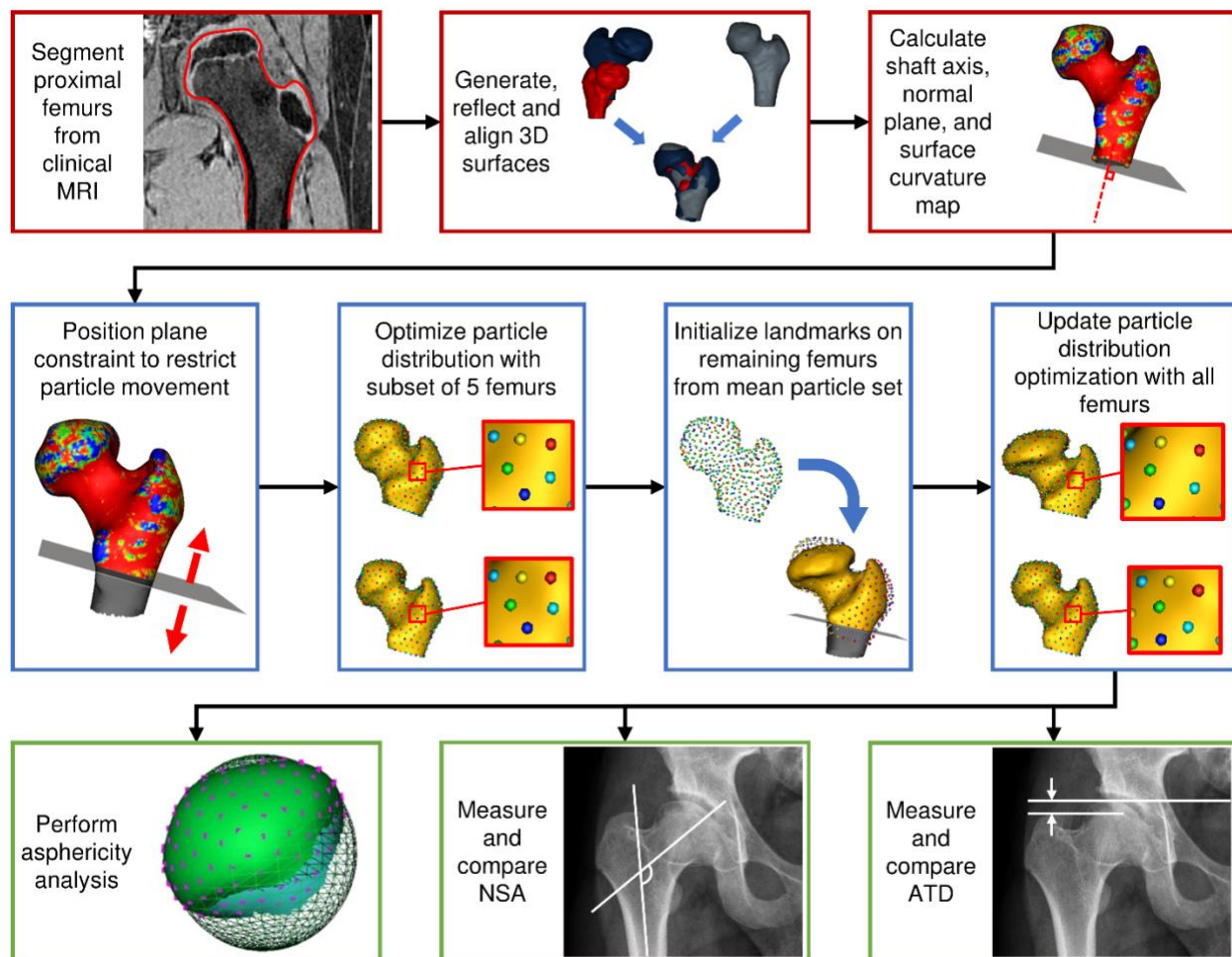
103 Abbreviations: NSA, neck-shaft angle; ATD, articular-trochanteric distance.

104

105 An MRI scan of the hip joints was obtained using a GE Hdx 1.5 Tesla scanner (Waukesha, WI, USA).[19] A fat-  
106 suppressed 3D spoiled gradient-echo sequence was used to acquire images coronally (repetition time = 8.9 ms, echo  
107 time = 2.8 ms, flip angle = 10°, bandwidth = 20.8 kHz, slice thickness = 1.0 mm, matrix = 288 x 288). Each image  
108 volume was resampled based on its smallest voxel dimension (0.47 – 0.63 mm) to produce an isotropic image  
109 volume for segmentation.

### 110 3.2 Framework Step 1: Segmentation

111 From the resampled images of each patient, the affected proximal femur (or femurs for the two patients with  
112 bilateral LCPD) was segmented to include the femoral head and approximately two centimetres of the proximal  
113 femoral shaft below the tip of the lesser trochanter (Figure 1). Segmentation was performed manually by two  
114 segmentation experts (LJ and SS). An initial segmentation pass of each proximal femur, focusing on anatomical  
115 accuracy, (LJ, *3D Slicer* v4.13.0, Slicer community, [www.slicer.org](http://www.slicer.org))[27] was followed by a refinement pass to  
116 correct any errors and remove voxel-scale surface roughness (SS, *Amira* v6.0.1, Thermo Fisher Scientific Inc.,  
117 Waltham, MA, USA). Due to the patients' varied stages of ossification, the segmentation protocol included isolation  
118 of both bone and cartilage of the proximal femoral epiphysis and apophyses of the greater and lesser trochanters, to  
119 better reflect the full shape of the bone (Figure 1). To assess the repeatability of the segmentation protocol between  
120 raters and software packages, each rater separately completed both segmentation passes on one femur, and the  
121 Hausdorff distance was calculated between the two segmentation boundaries.



122  
 123 **Fig. 1** Key stages of the modeling and analysis pipeline for this statistical shape model (SSM) framework, including  
 124 segmentation and surface mesh preparation steps (top row, red), the particle-based correspondence step using an  
 125 incremental optimization routine in *ShapeWorks* (middle row, blue), and analysis of anatomical variation (bottom  
 126 row, green).

### 127 3.3 Framework Step 2: Surface Mesh Preparation

128 Three-dimensional surfaces of the proximal femurs were generated in *Amira*, using a previously published iterative  
 129 smoothing and decimation protocol.[28] Due to the small size of the pediatric anatomy, meshes were scaled to three  
 130 times their native resolution to reduce the effective strength of particle repulsion and improve correspondence  
 131 optimization in the subsequent step. Meshes were reflected, if left-sided, and aligned via the iterative closest point  
 132 algorithm using *CloudCompare* v2.11 ([www.cloudcompare.org](http://www.cloudcompare.org))[29] (Figure 1).

133 Cutting planes were defined to constrain particle placement to consistent regions of the proximal femur. To do so,  
 134 the best-fit cylinder to the femoral shaft was determined for each mesh using custom *MATLAB* code (*MATLAB*  
 135 R2022a, The MathWorks Inc, Natick, Massachusetts, USA). The orientation of the long axis of the cylinder defined  
 136 the normal vector of the plane (Figure 1). Next, Gaussian curvature maps were computed for each mesh using  
 137 *MeshLab* (v2022.02, Visual Computing Lab, ISTI-CNR, Pisa, Italy), to guide the proximal/distal placement of the  
 138 plane in the particle-based correspondence step.[30]

### 139 3.4 Framework Step 3: Particle-based Correspondence

140 We used *ShapeWorks* v6.3.0 ([shapeworks.sci.utah.edu](http://shapeworks.sci.utah.edu))[12] on an ASUS GL552V laptop (Intel Core i7-6700-HQ,  
 141 Windows 10) to generate a particle-based correspondence model of the proximal femur. After importing the femur

142 surface meshes and cutting plane orientations generated in the previous steps, the proximal/distal position of the  
143 plane on each femur was standardized by using the distal part of the lesser trochanter physis when visible on MRI in  
144 conjunction with the division between the lesser trochanter and femoral shaft created by the curvature map (Figure  
145 1).

146 We utilized a two-stage incremental optimization approach to establish particle correspondence across the femoral  
147 meshes. Incremental optimization routines begin with initially fitting a model to a subset of the most similar shapes,  
148 before incrementally adding outlier shapes. In small datasets with large shape variance, incremental optimization  
149 can achieve better particle correspondence and model compactness compared to a model optimized on the whole  
150 dataset at once.[25] In the current study the first stage involved placing correspondence particles (n=512) on a subset  
151 of five meshes using a fully automated hierarchical splitting strategy and entropy-based optimization (Figure 1).[24]  
152 Generalized Procrustes analysis removed the effect of pose and scale during optimization of particle position. The  
153 mean particle coordinates from the first stage were used to initialize particle locations on the remaining eight  
154 meshes, after which the optimization routine was rerun in order to establish correspondence on all 13 surfaces  
155 (Figure 1).

156 Principal component analysis (PCA) was utilized to consolidate the dimensionality of the model (equal to the  
157 number of particles multiplied by the three spatial dimensions) to a set of linearly uncorrelated modes, which  
158 describe the dominant shape variations among the cohort. Patient-specific PCA component scores were used to  
159 describe the shape of each femur relative to the variation captured by each mode. Here, PCA scores can be  
160 understood as the weights for each variable when calculating the principal component.

### 161 3.5 *Framework Evaluation*

162 We evaluated our SSM framework performance using the three standard metrics: compactness, the proportion of  
163 total variability explained by a chosen number of modes; generalization, the ability of the model to represent shapes  
164 that were not part of the training set; and specificity, the ability of the model to generate only valid shapes and to  
165 differentiate between shapes in different categories.[31] To test our model's sensitivity to changes in training set  
166 size, we extended the generalization calculation from a leave-one-out to a leave-N-out cross validation using custom  
167 Python code. Values of generalization were calculated for  $N = 1$  to  $N = 9$  (an effective training set size of 12 and 4  
168 respectively); the case for  $N = 1$  is equivalent to the standard generalization metric.

### 169 3.6 *Analysis of Anatomical Variation*

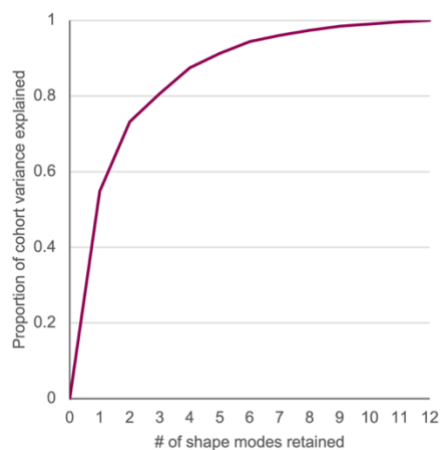
170 To explore how the current SSM framework may be applied alongside alternative 2D or 3D measures of deformity,  
171 we compared the PCA component scores for each femur in our evaluation cohort with a 3D measure of femoral head  
172 asphericity and 2D measurements from each patient's corresponding clinical radiographs. Gaussian curvature was  
173 computed for the reconstructed mean mesh in *MeshLab*, and used to extract the region corresponding to the femoral  
174 head in *CloudCompare* (Figure 1). The indices of the correspondence particles that resided within the mean femoral  
175 head region were then identified and used to calculate the best-fit sphere for each femoral head in the cohort using  
176 custom *MATLAB* code. Asphericity was expressed as the root-mean square error of the sphere fit (Table 1). Neck-  
177 shaft angle (NSA) and articulo-trochanteric distance (ATD) were measured on anterior-posterior radiographs for each  
178 patient femur (Figure 1, Table 1). Last, Spearman's rank correlation coefficient was quantified to examine the  
179 relationship between asphericity, NSA and ATD with PCA component scores.

## 180 4 **Results**

181 Figure 2 shows good performance of this SSM framework when applied to the evaluation cohort. The model is  
182 compact, representing almost 90% of the total variation with just four modes (Figure 2a). The model generalizes to  
183 less than 1mm with four modes (Figure 2b), with the generalization curve flattening after the ninth mode. The  
184 model's specificity is effectively constant (Figure 2c), with a range of 1.12-1.14mm.

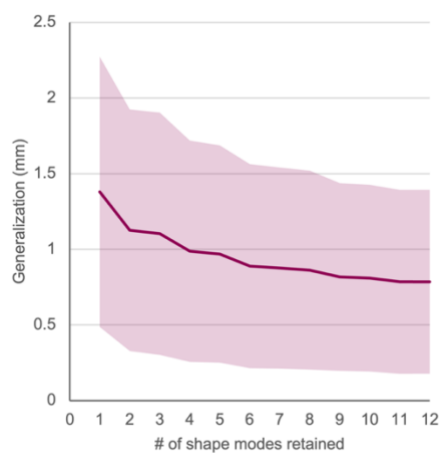
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186 a.



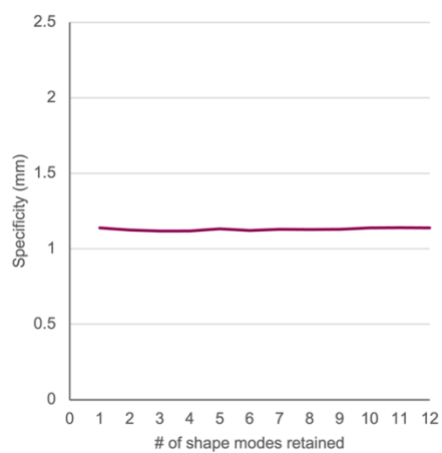
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188 b.



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190 c.



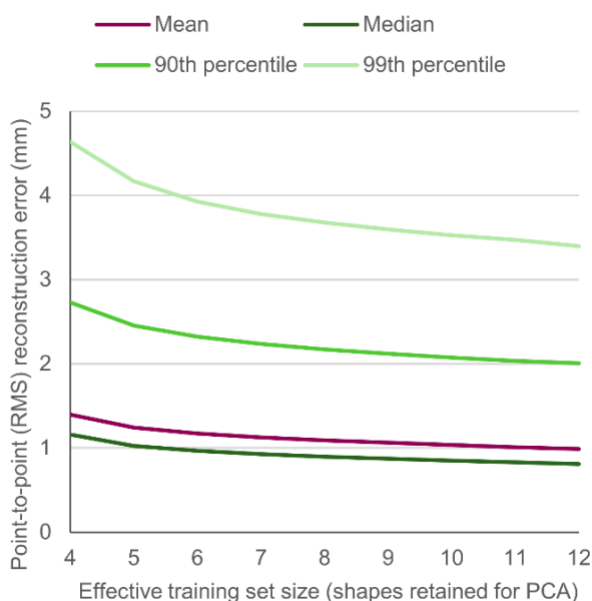
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192 **Fig. 2** Results of SSM evaluation when up to 12 shape modes are retained, presented using the three standard  
 193 evaluation metrics: **a) compactness**, the cumulative proportion of cohort variance explained; **b) generalization**, the  
 194 average point-to-point error when reconstructing unfamiliar shapes (shaded area indicates  $\pm 1$  standard deviation); **c)**

195 **specificity**, the average point-to-point difference between shapes randomly generated from the SSM and their  
 196 closest training set shapes.

197

198 Leave-N-out cross validation demonstrated the sensitivity of this framework to changes in the training set size when  
 199 four shape modes are included (Figure 3). Increasing N from 1 to 9 (reducing the effective training set size from 12  
 200 to 4 femurs) increased the mean point-to-point reconstruction error (generalization) from 0.99mm to 1.40mm. The  
 201 mean Hausdorff distance between segmentations completed separately by each rater (LJ and SS) on one femur was  
 202 0.38 mm (maximum 3.35 mm, 95<sup>th</sup> percentile 1.13 mm).



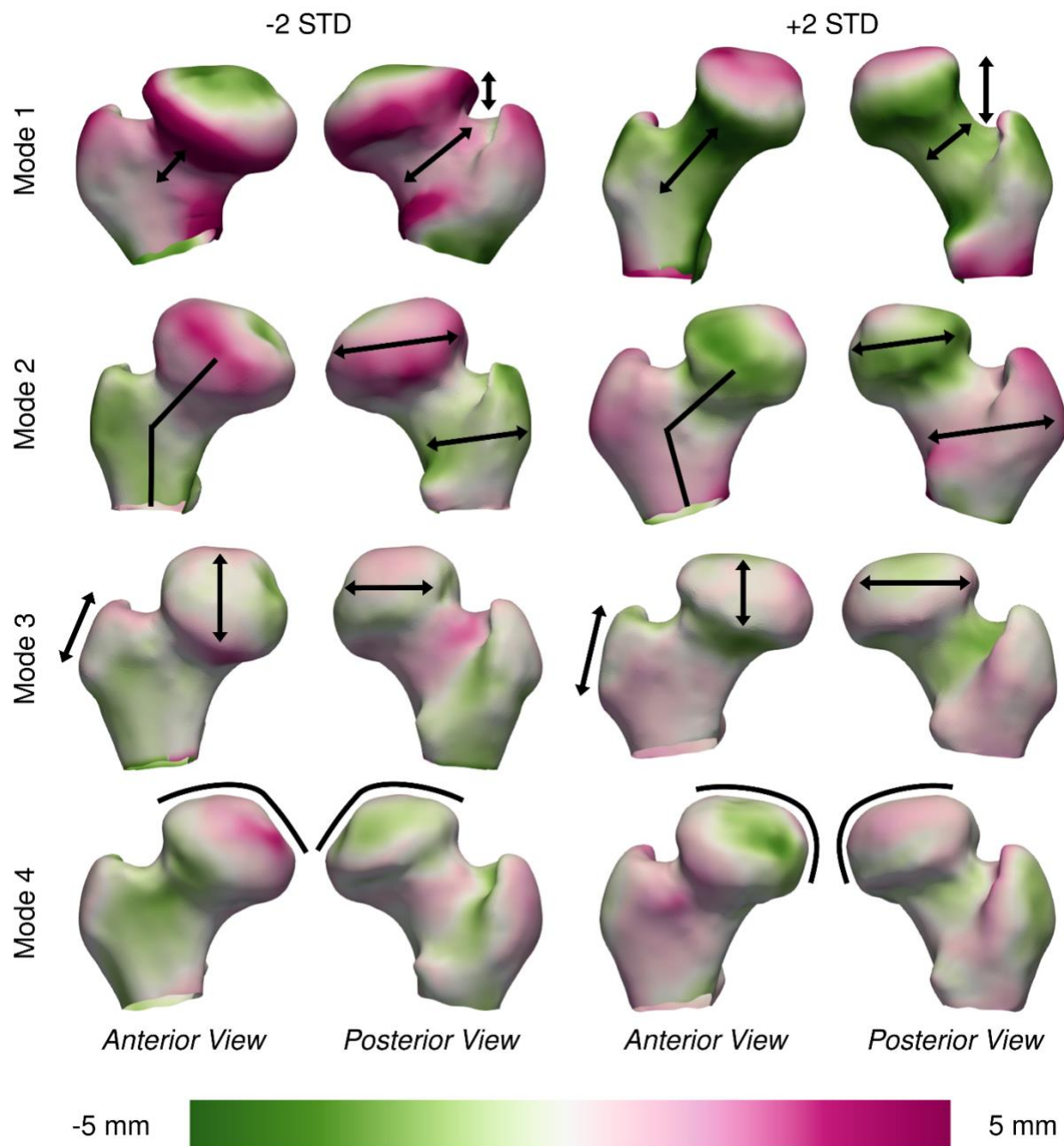
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204 **Fig. 3** Results of leave-N-out cross-validation evaluation of framework performance, showing the impact of changes  
 205 in the effective training set sample size on the mean (purple), median (dark green), 90<sup>th</sup> and 99<sup>th</sup> percentile (green  
 206 and light green, respectively) point-to-point reconstruction error using four shape modes.

207

208 The first four modes of variation were selected for further analysis, as these modes accounted for at least 5% of the  
 209 total variation observed in the SSM. Together, these modes accounted for 87.5% of the total cohort variability, with  
 210 generalization and specificity of 0.99mm and 1.12mm respectively. Mode I described the oblateness (the degree of  
 211 compression of a sphere, here along the axis of the femoral neck, to form an ellipsoid) and width of the femoral head  
 212 in the anterior-posterior and medial-lateral directions, vertical angle of the lateral greater trochanter, and ATD  
 213 (Figure 4). Mode II described the slope of the superior femoral head, size of the femoral head and greater trochanter,  
 214 ATD, NSA, prominence of the vastus ridge, and depth of the fovea (Figure 4). Mode III described the height of the  
 215 femoral head and vastus ridge, shape of the intertrochanteric crest, and width of the femoral neck (Figure 4). Lastly,  
 216 mode IV described anterior protrusion and asphericity of the femoral head, prominence of the posterior greater  
 217 trochanter, and NSA (Figure 4).





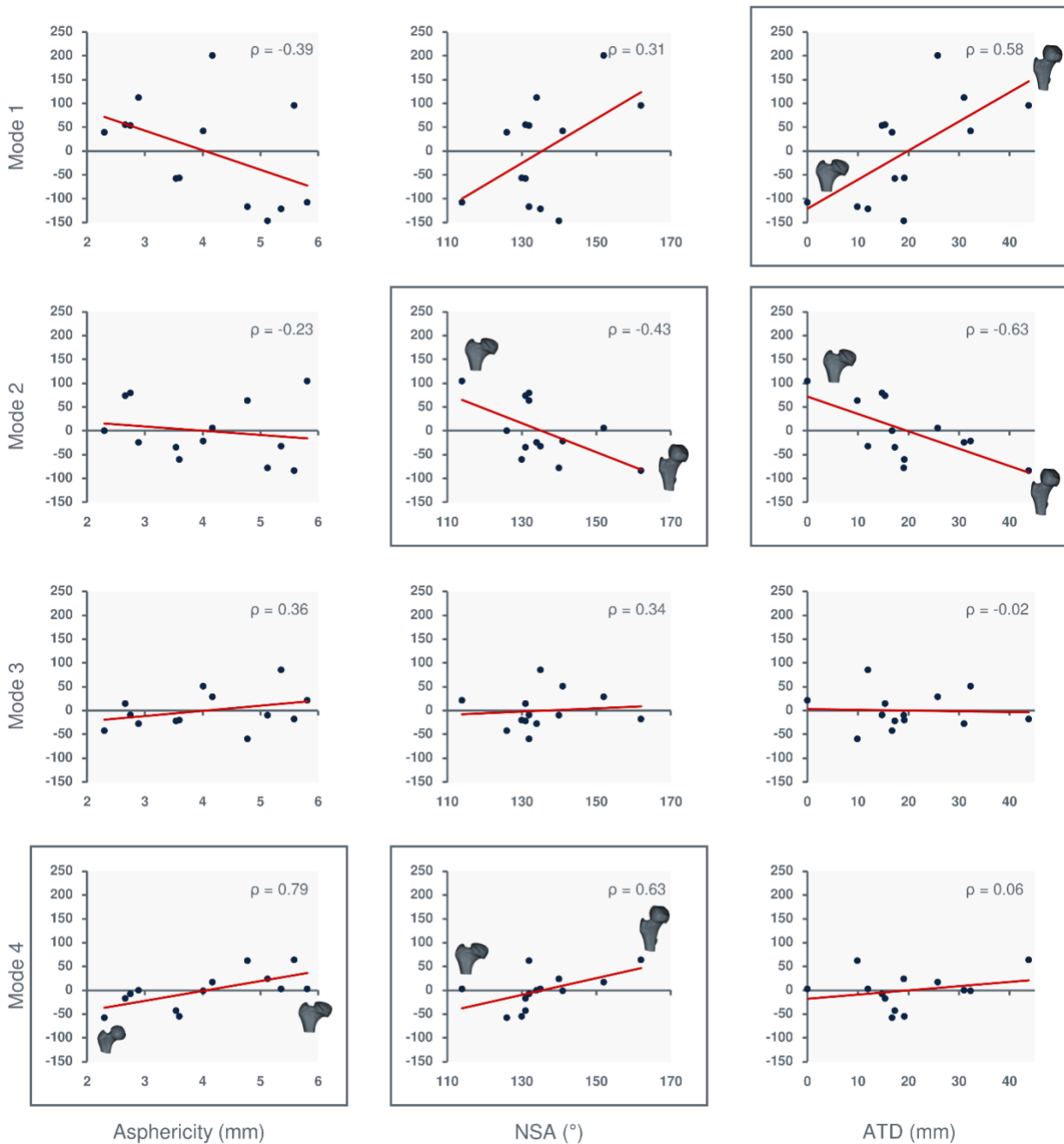
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219 **Fig. 4** The first four principal component analysis (PCA) modes of the evaluation statistical shape model (SSM).  
 220 Surface distance plots show shapes with each mode set to  $\pm 2$  standard deviations (SD) from the cohort mean shape,  
 221 and the deviation of each surface from the mean shape is represented by a color gradient from green (negative  
 222 displacement) to magenta (positive displacement). Arrows qualitatively represent notable areas of variation captured  
 223 by each mode.

224

225 Shape mode scores were calculated for each femur in the evaluation cohort and compared with the corresponding  
 226 femoral head asphericity, NSA, and ATD measurements for that femur (Figure 5). Correlations between shape mode  
 227 scores and these parameters ranged from very weak to strong. Asphericity and NSA were most strongly correlated  
 228 with mode IV (Spearman's rank correlation coefficients of 0.79 and 0.63 respectively), whereas ATD was most  
 229 strongly correlated with mode II (Spearman's rank correlation coefficient of -0.63). Other notable correlations where

230 Spearman's rank correlation coefficient was stronger than  $\pm 0.4$  included NSA with Mode II (-0.43) and ATD with  
 231 mode I (0.58).



232

233 **Fig. 5** Analysis of anatomical variation. Shape mode scores for each proximal femur in the evaluation cohort are  
 234 plotted on the vertical axes (rows from top to bottom representing modes 1-4), against femoral head asphericity (left  
 235 column), neck-shaft angle (NSA, middle column), and articular-trochanteric distance (ATD, right column).  
 236 Spearman's rank correlation coefficient ( $\rho$ ) is shown for each relationship, and relationships stronger than  $\rho = \pm 0.4$   
 237 are indicated with a plot boundary and depictions of the femurs with the highest and lowest horizontal axis values.

## 238 5 Discussion

239 In this study, we developed and implemented a new methodological framework for constructing SSM of highly  
 240 heterogeneous LCPD anatomy, based on progressive optimization of particle correspondences. We evaluated this  
 241 framework by producing a 3D SSM of proximal femurs from clinical MR images of patients in stage IIa-IV LCPD,  
 242 which provided a compact, accurate, and objective description of 3D shape and shape variation in LCPD. The first  
 243 four PCA components of this model met our threshold for inclusion (>5% of overall cohort variance); these modes  
 244 described morphological changes characteristic of LCPD consistent with clinical observation such as an enlarged  
 245 and widened FH and a high-riding greater trochanter. Quantitative associations between PCA component scores and  
 246 radiographic measurements demonstrated how to interpret SSM-based findings relative to clinical radiographic  
 247 measurements of LCPD that are more familiar to clinicians than SSM-based measurements.

248 The contribution of this work is a framework, which includes protocols for image volume segmentation, surface  
 249 mesh preparation, and generation of a particle-based correspondence model. The main steps of the current  
 250 framework are derived from existing protocols,[13, 28] with the key innovation of incremental optimization of  
 251 particle correspondences.[25] As well as improving performance in small and heterogeneous datasets, incremental  
 252 optimization also enables incremental expansion of the model using data from multiple sources. Open science  
 253 practices are a powerful tool to facilitate research into rare conditions such as LCPD, and every step in the  
 254 framework can be carried out using free and open source software (including *Octave*, an open-source  
 255 implementation of *MATLAB*). Collectively, the described framework and SSM results of this study provide a basis  
 256 for developing more standardized tools to evaluate LCPD deformity in 3D. Due to its compact but comprehensive  
 257 description of morphology, this modeling framework provides opportunities for future SSM research to relate  
 258 patient-specific morphology with biomechanics in affected and healthy participants, or to longitudinally quantify  
 259 how LCPD hips remodel in modified Waldenstrom stage IV until skeletal maturity.

260 In our small cohort of LCPD hips, the SSM framework produced a model with good evaluation results. A  
 261 compactness of 87.5% with four modes demonstrates efficient representation of the cohort’s variability. A  
 262 generalization below 1mm with four or more modes suggests that the model was robust when applied to unfamiliar  
 263 data, and was not over-fit to the training set. The specificity curve of the model did not meaningfully change with  
 264 the number of modes considered, which may be an artifact of the small size and heterogeneity of the training set. To  
 265 calculate specificity, *ShapeWorks* generates shapes by assigning random normally distributed shape mode weights.  
 266 However, no individual shape in our evaluation cohort is close to the average shape in the first mode (Figure 5). As  
 267 a result, the point-to-point distance between the large number of shapes generated near the mean and the relatively  
 268 distant “nearest” training set examples dominates the specificity calculation for all modes. The resultant specificity  
 269 of 1.1mm suggests that the model could nonetheless effectively discriminate between shapes and shape categories.

270 The accuracy of this evaluation model was better than other hip SSMs produced using larger training sets. For  
 271 example, Ziaeiipoor *et al.* reported a median generalization error of 1.1-4.6mm using a training set of 18 normal  
 272 femurs, and Whitmarsh *et al.* reported a mean reconstruction error of 1.1mm using 12 modes with a training set of  
 273 85 normal, osteopenic and osteoporotic femurs.[32, 33] In addition, our leave-N-out cross-validation analysis  
 274 suggests that the framework’s performance is robust to changes in training set sample size. Collectively, these  
 275 measures of SSM performance provide confidence in using the described framework to further study LCPD  
 276 pathomorphology.

277 Our results were broadly similar to studies by Chan *et al.*, who produced an SSM that included some LCPD  
 278 proximal femurs alongside those with slipped capital femoral epiphysis (SCFE) and no pathology.[17, 18] This  
 279 previous model exhibited similar features in shape modes associated with LCPD when compared to the present  
 280 study, including short and wide femoral necks and flattened heads as noted by Chan and colleagues. Similarity  
 281 between the previous and present models was particularly notable in mode I, whereas subsequent modes differ with  
 282 more characteristics of SCFE present in the previous model. We felt it was important to produce a new model using  
 283 only LCPD proximal femurs to evaluate our SSM framework as it is unclear how much of the variation described by  
 284 each mode can be attributed to LCPD as opposed to SCFE, particularly as LCPD proximal femurs made up only a  
 285 small proportion (one ninth) of the whole cohort in the study by Chan and colleagues ( $N_{LCPD} = 5$ ,  $N_{SCFE} = 19$ ,  $N_{healthy}$   
 286  $= 21$ ).

287 Correlations between PCA component scores and standard radiographic measures were evaluated to interpret each  
 288 significant mode of variation relative to existing clinical measures of deformity. In our evaluation cohort, NSA  
 289 appeared to prominently change in modes 1 and 2 of the model (Figure 4). However, the correlation between mode I

290 principal component score and clinically measured NSA was weak compared to ATD, a closely related  
 291 measurement (Figure 5). This may be caused by difficulty in measuring NSA in patients with short, wide femoral  
 292 necks, asymmetric femoral anteversion,[34] and an unclear femoral head center. This example demonstrates a  
 293 potential application of the framework: to evaluate radiographic measurements against a 3D baseline shape  
 294 description, which has been explored and validated in previous studies of the proximal femur.[13, 16] Harris *et al.*  
 295 (2013) applied a similar analysis to SSM of adult hips with cam FAI deformity,[13] and reported “moderate to  
 296 weak” associations between key radiographic metrics and shape modes (up to  $\rho=0.403$  for Mode 1 and alpha angle).  
 297 The stronger associations (up to  $\rho=0.79$ ) found in the present study demonstrate the large size of LCPD deformity  
 298 compared to FAI.

299 Representation of 3D pathomorphology in terms of continuous shape modes could improve the assessment of long-  
 300 term prognosis in the clinic. For example, in 2D SSM of adult hips, shape modes representing femoral neck length,  
 301 femoral neck width, and head-neck offset are predictive of total hip replacement.[15] Similarly, individual modes or  
 302 combinations of modes from SSM of LCPD deformity could predict the timing and severity of long-term outcomes  
 303 and inform preventative management strategies.

304 This study does have some considerations and limitations. First, we studied a small group of hips to evaluate the  
 305 framework in a cohort representative of LCPD morphology, and to illustrate how the resulting models may be  
 306 related to existing clinical measures. Readers should not draw clinical conclusions from these findings, and we have  
 307 not performed hypothesis testing for that purpose. A full assessment of LCPD pathomorphology should include age  
 308 groups at various stages of development, each consisting of patients with a representative range of disease severities.  
 309 The influence of factors such as the modality of the source imaging, resolution, and contrast on the performance of  
 310 the current framework should also be considered as part of future research. Second, the field of view of the  
 311 retrospective MR images did not include the distal femur or full hemipelvis, without which the model cannot  
 312 describe key features such as femoral version[34] or the pose-dependent relationship between the femoral head and  
 313 acetabulum. Future work making use of this SSM framework should ensure that all relevant anatomy is included in  
 314 the field of view, including both femurs to the knee joint and the full pelvis. Finally, the framework presented herein  
 315 does not itself separate changes in shape due to pathology from changes due to normal growth, the latter being  
 316 substantial in the population of interest. We believe that accurate representation of shape for the whole range of  
 317 deformity severity and at all developmental stages of growth will allow for more detailed studies of the relationship  
 318 between deformity and growth in future. Our framework report in this study is well placed to provide that shape  
 319 representation.

320 In summary, the methodological framework for SSM proposed in this study provides an accessible, compact and  
 321 accurate representation of the 3D pathomorphology of LCPD. This expandable framework represents a step towards  
 322 an objective standard for describing 3D LCPD morphology, which could help researchers and clinicians better  
 323 understand how pathomorphology affects long-term outcomes in patients. This understanding will facilitate the  
 324 development of patient-specific treatment guidelines for residual proximal femoral deformity, particularly in patients  
 325 who are at high risk of developing early-onset OA.

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